

|                     |               |                               |                        |
|---------------------|---------------|-------------------------------|------------------------|
| $tvar, b$           | type variable |                               |                        |
| $var, x$            | term variable |                               |                        |
| $const, c$          | term constant |                               |                        |
| $kind, K$           | $::=$         |                               |                        |
|                     |               | type                          |                        |
|                     |               | $\Pi x : T.K$                 |                        |
|                     |               | $K[\theta]$                   |                        |
|                     |               | $(K)$                         |                        |
| $type, T$           | $::=$         |                               |                        |
|                     |               | $b$                           |                        |
|                     |               | $T t$                         |                        |
|                     |               | $\Pi x : T.T'$                |                        |
|                     |               | $(T)$                         |                        |
|                     |               | $T[\theta]$                   |                        |
| $term, t$           | $::=$         |                               | term                   |
|                     |               | $x$                           | variable               |
|                     |               | $c$                           | constant               |
|                     |               | $\lambda x : T.t$             | bind $x$ in $t$ lambda |
|                     |               | $t t'$                        | app                    |
|                     |               | $(t)$                         |                        |
|                     |               | $t[\theta]$                   |                        |
| $signature, \Sigma$ | $::=$         |                               | signature              |
|                     |               | $\cdot$                       |                        |
|                     |               | $\Sigma, c : T$               |                        |
|                     |               | $\Sigma, b : K$               |                        |
| $context, \Gamma$   | $::=$         |                               | context                |
|                     |               | $\cdot$                       |                        |
|                     |               | $\Gamma, x : T$               |                        |
| $subst, \theta$     | $::=$         |                               |                        |
|                     |               | $\cdot$                       |                        |
|                     |               | $\theta, t/x$                 |                        |
| $terminals$         | $::=$         |                               |                        |
|                     |               | type                          |                        |
|                     |               | kind                          |                        |
|                     |               | $\lambda$                     |                        |
|                     |               | $\Pi$                         |                        |
|                     |               | $\cdot$                       |                        |
|                     |               | $\cdot$                       |                        |
|                     |               | $\cdot$                       |                        |
| $formula$           | $::=$         |                               |                        |
|                     |               | <i>judgement</i>              |                        |
|                     |               | <b>not</b> ( <i>formula</i> ) |                        |

*Jop* ::=

- |  $b \in \mathbf{dom}(\Sigma)$
- |  $c \in \mathbf{dom}(\Sigma)$
- |  $x \in \mathbf{dom}(\Gamma)$
- |  $\Sigma; \Gamma \vdash K \equiv K' : \text{kind}$
- |  $\Sigma; \Gamma \vdash T \equiv T' : K$
- |  $\Sigma; \Gamma \vdash t \equiv t' : T$
- |  $\vdash \Sigma \text{ sig}$
- |  $\Sigma \vdash \Gamma \text{ ctx}$
- |  $\Sigma; \Gamma \vdash K : \text{kind}$
- |  $\Sigma; \Gamma \vdash T : K$
- |  $\Sigma; \Gamma \vdash t : T$

*judgement* ::=

- | *Jop*

*user\_syntax* ::=

- | *tvar*
- | *var*
- | *const*
- | *kind*
- | *type*
- | *term*
- | *signature*
- | *context*
- | *subst*
- | *terminals*
- | *formula*

$b \in \mathbf{dom}(\Sigma)$

$\frac{}{b \in \mathbf{dom}(\Sigma, b : K)}$  BINSIG\_1

$\frac{b \in \mathbf{dom}(\Sigma)}{b \in \mathbf{dom}(\Sigma, b' : K)}$  BINSIG\_2

$\frac{b \in \mathbf{dom}(\Sigma)}{b \in \mathbf{dom}(\Sigma, c : T)}$  BINSIG\_3

$c \in \mathbf{dom}(\Sigma)$

$\frac{}{c \in \mathbf{dom}(\Sigma, c : T)}$  CINSIG\_1

$\frac{c \in \mathbf{dom}(\Sigma)}{c \in \mathbf{dom}(\Sigma, b : K)}$  CINSIG\_2

$\frac{c \in \mathbf{dom}(\Sigma)}{c \in \mathbf{dom}(\Sigma, c' : T)}$  CINSIG\_3

$x \in \mathbf{dom}(\Gamma)$

$\frac{}{x \in \mathbf{dom}(\Gamma, x : T)}$  XINCTX\_1

$$\frac{x \in \mathbf{dom}(\Gamma)}{x \in \mathbf{dom}(\Gamma, x' : T)} \quad \text{XINCTX\_2}$$

$$\boxed{\Sigma; \Gamma \vdash K \equiv K' : \text{kind}}$$

$$\frac{\vdash \Sigma \text{ sig} \quad \Sigma \vdash \Gamma \text{ ctx}}{\Sigma; \Gamma \vdash \text{type}[\theta] \equiv \text{type} : \text{kind}} \quad \text{sK\_1}$$

$$\frac{\Sigma; \Gamma \vdash T[\theta] \equiv T' : K'' \quad \Sigma; \Gamma \vdash K[\theta] \equiv K' : \text{kind}}{\Sigma; \Gamma \vdash (\Pi x : T.K)[\theta] \equiv (\Pi x : T'.K') : \text{kind}} \quad \text{sK\_2}$$

$$\boxed{\Sigma; \Gamma \vdash T \equiv T' : K}$$

$$\frac{\Sigma; \Gamma \vdash b : K}{\Sigma; \Gamma \vdash b[\theta] \equiv b : K} \quad \text{sT\_1}$$

$$\frac{\Sigma; \Gamma \vdash T[\theta] \equiv T' : (\Pi x : T.K) \quad \Sigma; \Gamma \vdash t[\theta] \equiv t' : T}{\Sigma; \Gamma \vdash (T t)[\theta] \equiv T' t' : K} \quad \text{sT\_2}$$

$$\frac{\Sigma; \Gamma \vdash T_1[\theta] \equiv T'_1 : \Pi x : T_2.K \quad \Sigma; \Gamma \vdash T_2[\theta] \equiv T'_2 : K_2}{\Sigma; \Gamma \vdash (\Pi x : T_1.T_2)[\theta] \equiv (\Pi x : T'_1.T'_2) : \Pi x : T'_1.K_2} \quad \text{sT\_3}$$

$$\boxed{\Sigma; \Gamma \vdash t \equiv t' : T}$$

$$\frac{\Sigma; \Gamma \vdash c : T}{\Sigma; \Gamma \vdash c[\theta] \equiv c : T} \quad \text{ST\_1}$$

$$\frac{\Sigma; \Gamma \vdash t : T}{\Sigma; \Gamma \vdash x[\theta, t/x] \equiv t : T} \quad \text{ST\_2}$$

$$\frac{\Sigma; \Gamma \vdash x[\theta] \equiv t : T}{\Sigma; \Gamma \vdash x[\theta, t'/x'] \equiv t : T} \quad \text{ST\_3}$$

$$\frac{\Sigma; \Gamma \vdash T[\theta] \equiv T' : K_2 \quad \Sigma; \Gamma \vdash t[\theta] \equiv t' : T_2}{\Sigma; \Gamma \vdash (\lambda x : T.t)[\theta] \equiv (\lambda x : T'.t') : T_3} \quad \text{ST\_4}$$

$$\frac{\Sigma; \Gamma \vdash t_1[\theta] \equiv t'_1 : T_1 \quad \Sigma; \Gamma \vdash t_2[\theta] \equiv t'_2 : T_2}{\Sigma; \Gamma \vdash (t_1 t_2)[\theta] \equiv t'_1 t'_2 : T_3} \quad \text{ST\_5}$$

$$\boxed{\vdash \Sigma \text{ sig}}$$

$$\frac{}{\vdash \cdot \text{sig}} \quad \text{SIG\_EMPTY}$$

$$\frac{\vdash \Sigma \text{ sig} \quad \Sigma; \cdot \vdash K : \text{kind} \quad \mathbf{not}(b \in \mathbf{dom}(\Sigma))}{\vdash \Sigma, b : K \text{ sig}} \quad \text{SIG\_TYPE}$$

$$\frac{\vdash \Sigma \text{ sig} \quad \Sigma; \cdot \vdash c : T \quad \mathbf{not}(b \in \mathbf{dom}(\Sigma))}{\vdash \Sigma, b : K \text{ sig}} \quad \text{SIG\_CON}$$

$\Sigma \vdash \Gamma \text{ ctx}$ 

$$\frac{\vdash \Sigma \text{ sig}}{\Sigma \vdash \cdot \text{ ctx}} \text{ CTX\_EMPTY}$$

$$\frac{\begin{array}{l} \vdash \Sigma \text{ sig} \\ \Sigma \vdash \Gamma \text{ ctx} \\ \Sigma; \Gamma \vdash A : K \\ \mathbf{not} (x \in \mathbf{dom}(\Gamma)) \end{array}}{\Sigma \vdash \Gamma, x : A \text{ ctx}} \text{ CTX\_VAR}$$

 $\Sigma; \Gamma \vdash K : \text{kind}$ 

$$\frac{\begin{array}{l} \vdash \Sigma \text{ sig} \\ \Sigma \vdash \Gamma \text{ ctx} \end{array}}{\Sigma; \Gamma \vdash \text{type} : \text{kind}} \text{ WFKIND\_TYPE}$$

$$\frac{\Sigma; \Gamma, x : T \vdash K : \text{kind}}{\Sigma; \Gamma \vdash \Pi x : T. K : \text{kind}} \text{ WFKIND\_PI\_K\_INTRO}$$

 $\Sigma; \Gamma \vdash T : K$ 

$$\frac{\begin{array}{l} \vdash \Sigma, b : K \text{ sig} \\ \Sigma, b : K \vdash \Gamma \text{ ctx} \end{array}}{\Sigma, b : K; \Gamma \vdash b : K} \text{ WFTYPE\_TVAR\_Z}$$

$$\frac{\begin{array}{l} \vdash \Sigma, b : K \text{ sig} \\ \Sigma; \Gamma \vdash b' : K' \end{array}}{\Sigma, b : K; \Gamma \vdash b' : K'} \text{ WFTYPE\_TVAR\_S}$$

$$\frac{\begin{array}{l} \Sigma; \Gamma \vdash T : K' \\ \Sigma; \Gamma \vdash K \equiv K' : \text{kind} \end{array}}{\Sigma; \Gamma \vdash T : K} \text{ WFTYPE\_T\_EQ}$$

$$\frac{\Sigma; \Gamma, x : T \vdash T' : K}{\Sigma; \Gamma \vdash \Pi x : T. T' : K} \text{ WFTYPE\_PI\_T\_INTRO}$$

$$\frac{\begin{array}{l} \Sigma; \Gamma \vdash T : \Pi x : B. K \\ \Sigma; \Gamma \vdash t : T' \end{array}}{\Sigma; \Gamma \vdash T t : K[\cdot, t/x]} \text{ WFTYPE\_PI\_T\_ELIM}$$

 $\Sigma; \Gamma \vdash t : T$ 

$$\frac{\Sigma \vdash \Gamma, x : T \text{ ctx}}{\Sigma; \Gamma, x : T \vdash x : T} \text{ WFTERM\_VAR\_Z}$$

$$\frac{\begin{array}{l} \Sigma \vdash \Gamma, x : T \text{ ctx} \\ \Sigma; \Gamma \vdash x' : T' \end{array}}{\Sigma; \Gamma, x : T \vdash x' : T'} \text{ WFTERM\_VAR\_S}$$

$$\frac{\begin{array}{l} \vdash \Sigma, c : T \text{ sig} \\ \Sigma, c : T \vdash \Gamma \text{ ctx} \end{array}}{\Sigma, c : T; \Gamma \vdash c : T} \text{ WFTERM\_CON\_Z}$$

$$\frac{\begin{array}{l} \vdash \Sigma, c : T \text{ sig} \\ \Sigma; \Gamma \vdash c' : T' \end{array}}{\Sigma, c : T; \Gamma \vdash c' : T'} \text{ WFTERM\_CON\_S}$$

Definition rules: 34 good 0 bad  
Definition rule clauses: 85 good 0 bad